



Seminar Summer Term 2024 Bayesian Optimization for HPO

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[?] Questions regarding the organization [60min] Bayesian Optimization for HPO [?] Your Questions [25min] How to give a good presentation [?] Your Questions





The Big Picture

>> What is this about?









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(Hyper-) Parameters

>> What can we tune? What should we tune?





Modelparametersoptimizedduringtraining;output of the training.

Examples:

- **Splits** of a Tree
- Weights of a NN
- Coefficients of a linear model

Hyperparameters

set before training; control flexibility, structure and complexity of the model/ training procedure and performance

Examples:

- Learning Rate for XGBoost
- Kernel Type for GPs
- #Layers for ANNs

Can be **real-valued**, **integer**, **categorical** and **hierarchically dependent** on each other











How do we optimize it?

>> Here's my algorithm, data, metric and search space, what should I do?



















Advantages

- Very easy to implement
- Very easy to parallelize
- Can handle all types of hyperparameters

Disadvantages

- Scales badly with #dimensions
- Inefficient: Searches irrelevant areas
- Requires to manual define discretization
- All grid points need to be evaluated

















With a **budget** of T iterations:

- Grid Search evaluates T^{1/d}
- Random Search evaluates (most likely) T

unique values per hyperparameter dimension



Image source: [Hutter et al. 2019]

 \rightarrow Grid search can be disadvantageous if some hyperparameters have little of no impact on the performance [Bergstra et al. 2012]





Questions?





How do we optimize it efficiently?

>> Here's my algorithm, data and design space and I have only limited time, what should I do?







Photo by <u>Wilhelm Gunkel</u> on <u>Unsplash</u> Image by Feurer, Hutter: Hyperparameter Optimization. In: Automated Machine Learning



























General approach

- Fit a probabilistic model to the collected function samples (λ, c(λ))
- Use the model to guide optimization, trading off exploration vs exploitation

Popular approach in the statistics literature since Mockus et al. [1978]

- Efficient in #function evaluations
- Works when objective is nonconvex, noisy, has unknown derivatives, etc.
- Recent convergence results

[Srinivas et al. 2009; Bull et al. 2011; de Freitas et al. 2012; Kawaguchi et al. 2015]





BO loop **Require:** Search space Λ , cost function c, acquisition function u predictive model \hat{c}_i maximal number of function evaluations T **Result** : Best configuration $\hat{\lambda}$ (according to \mathcal{D} or \hat{c}) 1 Initialize data $\mathcal{D}^{(0)}$ with initial observations 2 for t = 1 to T do Fit predictive model $\hat{c}^{(t)}$ on $\mathcal{D}^{(t-1)}$ 3 Select next query point: $\boldsymbol{\lambda}^{(t)} \in \arg \max_{\boldsymbol{\lambda} \in \boldsymbol{\Lambda}} u(\boldsymbol{\lambda}; \mathcal{D}^{(t-1)}, \hat{c}^{(t)})$ 4 Query $c(\boldsymbol{\lambda}^{(t)})$ 5 Update data: $\mathcal{D}^{(t)} \leftarrow \mathcal{D}^{(t-1)} \cup \{ \langle \boldsymbol{\lambda}^{(t)}, c(\boldsymbol{\lambda}^{(t)}) \rangle \}$ 6





• Bayesian optimization uses Bayes' theorem:

$$P(A|B) = \frac{P(B|A) \times P(A)}{P(B)} \propto P(B|A) \times P(A)$$

• Bayesian optimization uses this to compute a posterior over functions:

$$P(f|\mathcal{D}_{1:t}) \propto P(\mathcal{D}_{1:t}|f) \times P(f), \quad \text{where } \mathcal{D}_{1:t} = \{ \lambda_{1:t}, c(\lambda_{1:t}) \}$$

Meaning of the individual terms:

- P(f) is the prior over functions, which represents our belief about the space of possible objective functions before we see any data
- $\mathcal{D}_{1:t}$ is the data (or observations, evidence)
- $P(\mathcal{D}_{1:t}|f)$ is the likelihood of the data given a function
- $P(f|\mathcal{D}_{1:t})$ is the posterior probability over functions given the data



Advantages

- Sample efficient
- Can handle noise
- Priors can be incorporated
- Does not require gradients
- Theoretical guarantees

Many extensions available: Multi-Objective | Multi-Fidelity | Parallelization | Warmstarting | etc.

Disadvantages

- Overhead because of model training
- Crucially relies on robust surrogate model
- Has quite a few design decisions





The acquisition function:

- decides which configuration to evaluate next
- judges the utility (or usefulness) of evaluating a configuration (based on the surrogate model)
- \rightarrow It needs to trade-off exploration and exploitation
 - Just picking the configuration with the lowest prediction would be too greedy
 - It needs to consider the uncertainty of the surrogate model







Given some observations and a fitted surrogate,







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We care about *improving* over the c_{inc}.







We care about *improving* over the c_{inc} .







Let's look at a candidate configuration $\boldsymbol{\lambda}_1$ and its hypothetical cost c.







We can compute the improvement $I_c(\lambda_1)$. But how likely is it?







Knowing that $\hat{c}(\boldsymbol{\lambda}) = \mathcal{N}(\mu(\boldsymbol{\lambda}), \sigma^2(\boldsymbol{\lambda}))$, we can compute $p(c|\boldsymbol{\lambda})$

Comparing this for different configurations

and costs.

To compute EI, we sum all $p(c \mid \lambda) \times I_c$ over all possible cost values.

We define the one-step positive improvement over the current incumbent as

$$I^{(t)}(\boldsymbol{\lambda}) = \max(0, c_{inc} - c(\boldsymbol{\lambda}))$$

Expected Improvement is then defined as

$$u_{EI}^{(t)}(\boldsymbol{\lambda}) = \mathbb{E}[I^{(t)}(\boldsymbol{\lambda})] = \int_{-\infty}^{\infty} p^{(t)}(c \mid \boldsymbol{\lambda}) \times I^{(t)}(\boldsymbol{\lambda}) \ dc.$$

Choose
$$\boldsymbol{\lambda}^{(t)} \in \operatorname*{arg\,max}_{\boldsymbol{\lambda} \in \boldsymbol{\Lambda}}(u^{(t)}_{EI}(\boldsymbol{\lambda}))$$

- **Improvement-based** policies [Expected Improvement (EI), Probability of Improvement (PI), and Knowledge Gradient]
- **Optimistic** policies [Upper/Lower Confidence Bound (UCB/LCB)]
- Information-based policies [Entropy Search (ES)]
 - aim to increase certainty about the location of the minimizer
 - not necessarily evaluate promising configurations
- Methods combining/mixing/switching these

Questions?

- Gaussian Processes
- Random Forests
- Bayesian Neural Networks

Photo by <u>Filip Zrnzević</u> on <u>Unsplash</u> Photo by <u>Alina Grubnyak</u> on <u>Unsplash</u>

 $\begin{aligned} m(\mathbf{x}) &= \mathbb{E}[f(\mathbf{x})] \\ k(\mathbf{x}, \mathbf{x}') &= \mathbb{E}\left[(f(\mathbf{x}) - \mathbb{E}[f(\mathbf{x})]) \left(f(\mathbf{x}') - \mathbb{E}[f(\mathbf{x}')] \right) \right] \\ f(\mathbf{x}) \sim \mathcal{G}\left(m(\mathbf{x}), k\left(\mathbf{x}, \mathbf{x}'\right) \right) \end{aligned}$

Advantages

- Smooth uncertainty estimates
- Strong sample efficiency
- Expert knowledge can be encoded in the kernel
- Accurate predictions

Disadvantages

- Cost scales cubically with #observations
- Weak performance for high dimensionality
- Not easily applicable in discrete, categorical or conditional spaces
- Sensitive wrt its own hyperparameters

→ These make GPs the most commonly used model for Bayesian optimization

Advantages

- Scales well with #dimensions and #observations
- Training can be parallelized and is fast
- Can easily handle discrete, categorical and conditional spaces
- Robust wrt. its own hyperparameters

Disadvantages

- Poor uncertainty estimates
- Poor extrapolation (constant)
- Expert knowledge can not be easily incorporated

→ These make RFs a robust option in high dimensions, a high number of evaluations and for mixed spaces

Photo by <u>Filip Zrnzević</u> on <u>Unsplash</u> Photo by <u>Alina Grubnyak</u> on <u>Unsplash</u>

Image source: [Blundell et al. 2015]

Advantages

- Scales linear #observations
- (Can yield) smooth uncertainty estimates
- Flexibility wrt. discrete and categorical spaces

Disadvantages

- Needs many #observations
- Uncertainty estimates often worse than for GPs
- Many hyperparameters
- No robust off-the-shelf model

→ These make BNNs a promising alternative. [Li et al. 2023]

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Questions?

How to evaluate ML models when using HPO?

We want solutions that generalize to new data!

- \rightarrow "reasonable" predictions on **new data**
- This might include:
 - ignoring outliers
 - o smooth
 - capturing general trend

Source: Kaushik, 2016

Image: Bischl et al. 2023

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Questions?

Introduction to Bayesian Optimization

- R. Garnett "Bayesian Optimization" (2023) <u>https://bayesoptbook.com/</u>
- P. Frazier "A tutorial on Bayesian Optimization" (2018) <u>https://arxiv.org/abs/1807.02811</u>
- B. Bischl et al. "Hyperparameter Optimization: Foundation, Algorithms, Best Practuces and Open Challenges" <u>https://arxiv.org/pdf/2107.05847.pdf</u>

Some homework:

- 1. (recommended) Watch/Read intro to LLMs and transformers
 - A. Karpathy <u>https://www.youtube.com/watch?v=zjkBMFhNj_g</u>
 - L. Beyer <u>https://www.youtube.com/watch?v=Eixl6t5oif0</u>
 - Vaswani et al. "Attention is all you need" (2017) -<u>https://proceedings.neurips.cc/paper_files/paper/2017/hash/3f5ee243547dee91fbd05</u> <u>3c1c4a845aa-Abstract.html</u>
- 2. Send me any question you might have
- 3. Think of at least one use case for pre-trained models for AutoML and vice versa (!)

Note: You can look into "AutoML in the Age of LLMs - <u>https://arxiv.org/abs/2306.08107</u>", but try to think about it first. Only read "Callenges", "Opportunities" and "Risks"; no need to understand details about methods yet, this will be handled in the presentations.

Next week:

- Clarification/finalization of orga / topics / dates
- Answering your questions
- Discuss the applications you came up with